

## Isothermal Modelling of the Adsorption of Crystal violet onto Modified Charred Rice Husk

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### HISTORY

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### ABSTRACT

The rice milling process produces rice husk as a by-product. It is one of the most important agricultural leftovers in terms of volume. The data of the sorption isotherm of crystal violet (CV) sorption onto modified charred rice husk, which was plotted using linearized plots of isothermal models were reanalyzed using twenty isothermal models using nonlinear regression. Nineteen models — Henry, Langmuir, Freundlich, Jovanovic, Redlich-Peterson, Sips, Toth, Hill, Khan, BET, Vieth-Sladek, Radke-Prausnitz, Fritz-Schlunder III, Unilan, Baudu, Marczewski-Jaroniec, Fritz-Schlunder IV, Weber-van Vliet and Fritz-Schlunder V – fitted the data best using nonlinear regression. Statistical analysis based on error function analyses such as root-mean-square error (RMSE), adjusted coefficient of determination ( $\text{adj}R^2$ ), accuracy factor (AF), bias factor (BF), Bayesian Information Criterion (BIC), corrected AICc (Akaike Information Criterion), and Hannan-Quinn Criterion (HQC) showed that Jovanovic model was the best model. The maximal adsorption capacity in the Jovanovic model, expressed in milligrams per gram (mg/g), is denoted by  $q_{mj}$  while  $K_j$  is the Jovanovic constant, and the calculated values were 55.979 mg/L (95% confidence interval; 52.556 to 59.403) and 0.010 (95% confidence interval; 0.008 to 0.012), respectively. The nonlinear regression method provides parameter values within the 95% confidence interval, facilitating improved comparability with prior research.

### INTRODUCTION

Dye users provide color to textiles, paper, leather, and other materials to beautify and preserve them, therefore the environmental pollution and health risks of dye contamination are of great concern in nearly all nations in the developing world [1]. A dye is a powdered material that is mixed with another product or dissolved in a liquid (like paint or ink). Pigments are dispersed solids that are often powdered [2]. Both natural and synthetic dyes see extensive use because to their decorative and protective qualities. Once easily extracted from their complex mixtures, natural dyes are now notoriously finicky and time-consuming to isolate. These hues also inspired the development of modern synthetic dyes. Dyes are unique among organic compounds in that they absorb light in the visible spectrum due to their conjugated structure, chromophores, and absorbing chromophores [3]. It is a significant difficulty to remove color

from wastewater containing dyes using conventional treatment methods. Fish and other aquatic organisms are put at risk by the toxic organic compounds found in the wastewater discharged into rivers during the dye manufacturing and textile finishing processes [4]. Dyestuffs, textiles, paper, and plastics are just a few examples of sectors that rely on color. They create significant quantities of colored effluent byproducts, which eventually drain into water sources [3]. Such technological advances in industry, whether deliberate or accidental, have contributed to rising pollution levels as cities and populations have expanded. In order to prevent the release of industry waste effluents into the environment, textile companies must treat their effluents before releasing them [5]. When water is contaminated by synthetic color molecules, it has negative effects on both the environment and human health.

Dye runoff contributes to eutrophication and is a kind of aesthetic pollution. Textiles, leather, paper, paint, acrylic, cosmetics, plastic, medications, and other products that rely on dyes to provide color are essential to society. They drink a lot of water as well [6]. This results in copious volumes of discolored wastewater. Therefore, this research was carried out to lessen the prevalence of potentially harmful color pollution in potable water.

Wastewater cannot be discharged until all dyes have been removed. Chemical oxidation using chlorine and ozone, and adsorption techniques using alum, lime, ferric sulfate, and ferric chloride are also viable options [7,8], membrane separation processes [9,10], and adsorption [9,10]. The most promising therapies appear to be those based on adsorption. Recent years have seen a rise in the use of physicochemical methods including adsorption and electrochemical coagulation. Adsorption's convenience and versatility have contributed to its rising popularity [11,12].

Biological degradation, membrane filtration, and ion exchange are some more options besides oxidation by ozone or hydrogen peroxide [13,14], electrochemical oxidation [13], reverse osmosis [15], photocatalytic degradation [15], and adsorption [15]. Dye removal has been attempted using a number of various methods. There is a wide range of strategies for removing colors, each with its own cost in time and money.

The equilibrium, kinetic, and thermodynamic aspects of CV dye adsorption on modified rice husk (NMRH) were studied by Chakraborty et al. in 2011 [16]. The adsorption of CV dye on chemically modified rice husk (CMRH) was also the subject of an experimental batch research by Das et al. in 2012 [17]. The CMRH adsorbent was the most effective.

To remove the CV dye from water, adsorbent nanoparticles containing rice husk (TARH) were utilized [18]. An improved magnetic biochar nanocomposite (MBC) was developed by combining rice husk and iron oxide nanoparticles (IONPs), and its efficacy in either reducing CV dye in aqueous solutions or completely removing it was evaluated [19]. The effectiveness of NaOH-modified rice husk in adsorbing CV dye from aqueous solution was evaluated in laboratory-scale fixed-bed columns [20]. It has been discovered that RHC can absorb CV color from water [3].

In one experiment, bio-nanosilica was extracted from rice husk using ultrasonic technology, and CV dye was adsorbed onto aqueous effluents [21]. In order to remove the colour from the water, rice husk (RH) was utilized. Z-RHA, or zeolites mediated by rice husk ash, were created by a chemical alteration, and studies comparing their efficacy in cleaning up CV dye-tainted water were carried out [22]. According to the literature [11], Using RH as an adsorbent, which was easily accessible and cheap, CV could be removed from wastewater. RHC was also used to eliminate the CV dye.

The effects of other variables, such as agitation time, pH, and adsorbent concentration, have also been investigated [3]. Succinic acid-treated rice husk has been found to be effective at bleaching aqueous solutions [23]. The adsorption pattern of CV dye on succinic acid-treated rice husk was also assessed using a cyclic voltammetry method. Because of this, the oxidation and reduction signal both got bigger, and an oxidation peak showed up.

In order to get rid of CV dye in water, Van Hung synthesized nanosilica from rice husk [3]. The rice husk was "turned on" with nitric acid. Crystal violet-containing wastewater adsorption capacity was evaluated [24]. CV dye was shown to be effectively removed from aqueous solutions by using rice husk, sodium carbonate, and potassium hydrogen phosphate. Raw rice husk (RRH) is not an effective biosorbent since the process of dye adsorption onto it increases the chemical oxygen demand (COD) of the treated effluent. They also remove colors from treated wastewater while decreasing COD. A chemical oxygen demand (COD) analysis should be done to evaluate the biosorbent [3].

Crystal violet, like many other synthetic hues, is not biodegradable, is toxic, causes mutations and cancer, and can trigger allergies and skin rashes even in minute doses. Crystal violet can cause stomach upset, diarrhea, and gastritis if taken orally. Ingestion of large quantities can lead to nausea, abdominal pain, vomiting, severe headaches, chest pain, profuse sweating, confusion, painful urination, and hemoglobinemia. Crystal violet is toxic if ingested and can cause nausea, vomiting, and diarrhea if inhaled. Mucous membrane and gastrointestinal tract damage can occur with prolonged exposure [25].

Accurate assignment of adsorption kinetics and isotherms is essential for understanding the adsorption process in this context. The clearly nonlinear curve in this data is often presented in the literature with a linearized form. Because the error structure of the data changes when nonlinear data is linearized, estimating uncertainty is more challenging [26]. In this study, the published data from Chrystal violet dye adsorption onto charred rice husk was modelled with various isothermal models (**Table 1**) as well as regressed by the method of nonlinear regression. Best-fitted isotherm assessment was conducted using several error function analyses.

## METHOD

### Data acquisition and fitting

Figure 7 data from a previously published study [3] was digitized using the freeware Webplotdigitizer 2.5 [27]. After that, the data were nonlinearly regressed using the curve-fitting program Curve-Expert Professional (Version 1.6). Digitization using this program has been praised for its dependability [28,29].

### Statistical analysis

A set of statistical discriminatory tests such as corrected AICc (Akaike Information Criterion), Bayesian Information Criterion (BIC), Hannan and Quinn's Criterion (HQ), Root-Mean-Square Error (RMSE), bias factor (BF), accuracy factor (AF) and adjusted coefficient of determination ( $R^2$ ) were used in this study.

**Table 1.** Mathematical models that were used in modelling data [30,31].

| Isotherm             | p | Formula  | Ref.    |
|----------------------|---|--|---------|
| Henry's law          | 1 | $q_e = HC_e$   | [32]    |
| Langmuir             | 2 | $q_e = \frac{q_{mL} b_L C_e}{1 + b_L C_e}$   | [30]    |
| Jovanovic            | 2 | $q_e = q_{mJ}(1 - e^{-K_J C_e})$   | [33]    |
| Freundlich           | 2 | $q_e = K_F C_e^{\frac{1}{n_F}}$  | [34]    |
| Temkin               | 3 | $q_e = \frac{RT}{b_T} \{ \ln(a_T C_e) \}$  | [35]    |
| Dubinin-Radushkevich | 2 | $q_e = q_{mDR} \exp \left\{ -K_{DR} \left[ RT \ln \left( 1 + \frac{1}{C_e} \right) \right]^2 \right\}$         | [36,37] |
| Redlich-Peterson     | 3 | $q_e = \frac{K_{RP1} C_e}{1 + K_{RP2} C_e^{\beta_{RP}}}$   | [38]    |
| Sips                 | 3 | $q_e = \frac{K_S q_{mS} C_e^{\frac{1}{n_S}}}{1 + K_S C_e^{\frac{1}{n_S}}}$                                     | [39]    |
| Toth                 | 3 | $q_e = \frac{q_{mT} C_e}{(K_T + C_e^{n_T})^{1/n_T}}$   | [40]    |
| Hill                 | 3 | $q_e = \frac{q_{mH} C_e^{n_H}}{K_H + C_e^{n_H}}$   | [9]     |
| Khan                 | 3 | $q_e = \frac{q_{mK} b_K C_e}{(1 + b_K C_e)^{\alpha_K}}$  | [41]    |
| BET                  | 3 | $q_e = \frac{q_{mBET} \alpha_{BET} C_e}{(1 - \beta_{BET} C_e)(1 - \beta_{BET} C_e + \alpha_{BET} C_e)}$        | [42]    |
| Vieth-Sladek         | 3 | $q_e = \frac{q_{mVS} b_{VS} C_e}{(1 + b_{VS} C_e)^{n_{VS}}}$   | [43]    |
| Radke-Prausnitz      | 3 | $q_e = \frac{q_{mRP} K_{RP} C_e}{(1 + K_{RP} C_e)^{n_{RP}}}$   | [44]    |
| Brouers-Sotolongo    | 3 | $q_e = q_{mBS} (-K_{BS} C_e)^{-n_{BS}}$  | [45]    |
| Fritz-Schlunder-III  | 3 | $q_e = \frac{q_{mFS} K_{FS} C_e}{1 + K_{FS} C_e^{n_{FS}}}$   | [46]    |
| Unilan               | 3 | $q_e = \frac{q_{mU}}{2b_U} \ln \left( \frac{a_U + C_e e^{b_U}}{a_U + C_e e^{-b_U}} \right)$                    | [15]    |
| Baudu                | 4 | $q_e = \frac{q_{mB} b_B C_e^{(1+x+y)}}{1 + b_B C_e^{(1+x)}}$   | [47]    |
| Marczewski-Jaroniec  | 4 | $q_e = q_{mMJ} \left( \frac{(K_{MJ} C_e)^{n_{MJ}}}{1 + (K_{MJ} C_e)^{n_{MJ}}} \right)^{\frac{m_{MJ}}{n_{MJ}}}$ | [48]    |
| Fritz-Schlunder-IV   | 4 | $q_e = \frac{A_{FS} C_e^{B_{FS}}}{1 + B_{FS} C_e^{B_{FS}}}$  | [46]    |
| Weber-van Vliet      | 4 | $C_e = P_1 q_e^{(P_2 q_e^{P_3} + P_4)}$  | [49]    |
| Fritz-Schlunder-V    | 5 | $q_e = \frac{q_{mFVS} K_1 C_e^{\alpha_{FVS}}}{1 + K_2 C_e^{\beta_{FVS}}}$                                      | [46]    |

The RMSE was computed using Equation 1, and it stands to reason that the fewer parameters utilized, the smaller the RMSE will be. n is for the total number of observations made in the experiment, Obi and Pdi stand for the total number of observations made in the experiment and projections, and p stands for the total number of parameters [26].

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (Pd_i - Ob_i)^2}{n-p}} \quad (\text{Eqn. 1})$$

Because  $R^2$  or the coefficient of determination ignores the number of parameters in a model, the modified  $R^2$  is used to overcome this limitation. The entire variance of the y-variable is given by  $S^2_y$  in the equation (Equations 2 and 3), while RMS is the Residual Mean Square.

$$\text{Bias factor} = 10 \left( \sum_{i=1}^n \log \frac{(Pd_i / Ob_i)}{n} \right) \quad (\text{Eqn. 2})$$

$$\text{Accuracy factor} = 10 \left( \sum_{i=1}^n \log \frac{|(Pd_i / Ob_i)|}{n} \right) \quad (\text{Eqn. 3})$$

The AICc is computed as follows (Equation 4), where p represents the number of parameters and n represents the number of data points. The corrected Akaike information criterion (AICc) is used to manage data with a large number of parameters but a limited number of values [50]. A model with a lower AICc score is considered more likely to be right [50]. The information theory is the foundation of the Akaike Information Criterion (AIC). It strikes a compromise between the goodness of fit of a given model and the model's complexity [51].

$$AICc = 2p + n \ln \left( \frac{RSS}{n} \right) + \frac{2(p+1)+2(p+2)}{n-p-2} \quad (\text{Eqn. 4})$$

Another statistical tool based on information theory apart from AICc, is the Bayesian Information Criterion (BIC) (Equation 5). The number of parameters is penalized more severely by this error function than by AIC [27].

$$BIC = n \ln \left( \frac{RSS}{n} \right) + k \ln(n) \quad (\text{Eqn. 5})$$

The Hannan-Quinn information criterion (HQC) (Equation 6) is another error function approach based on information theory. Because of the  $\ln \ln n$  element in the calculation, the HQC is more consistent than the AIC [50].

$$HQC = n \ln \left( \frac{RSS}{n} \right) + 2k \ln(\ln n) \quad (\text{Eqn. 6})$$

The Accuracy Factor (AF) and Bias Factor (BF) are two further error function analyses derived from Ross's work [50]. These error functions evaluate models statistically for goodness-of-fit but do not penalize for the number of parameters (Equations 7 and 8).

$$\text{Adjusted } (R^2) = 1 - \frac{RMS}{S^2_y} \quad (\text{Eqn. 4})$$

$$\text{Adjusted } (R^2) = 1 - \frac{(1-R^2)(n-1)}{(n-p-1)} \quad (\text{Eqn. 5})$$

## RESULTS AND DISCUSSION

The equilibrium data from [3] was analyzed using fifteen models—Henry, Langmuir, Freundlich, Redlich-Petersen, Sips, BET, Toth, Hill, Khan, Vieth-Sladek, Radke-Prausnitz, Unilan, Fritz-Schlunder III, Fritz-Schlunder IV, and Fritz-Schlunder V, were used in finding the best fit by utilizing non-linear regression. Henry, Langmuir, Hill, Vieth-Sladek, Unilan, Sips and BET does not fit well with the data, whereas Freundlich, Redlich-Petersen, Toth, Khan, Radke-Prausnitz, Fritz-Schlunder III, Fritz-Schlunder IV, and Fritz-Schlunder V, fitted well with the data (Figs. 1 – 19).

The best isotherm model was found to be the Jovanovic with the lowest RMSE and AF, BF and  $\text{adj}R^2$  values closest to unity and lowest BIC, HQC and AICc values followed (descending order) by Langmuir, Sips, Hill and Redlich-Petersen (Table 2). As enough models fitted well with the charred rice husk data, it explains and justifies the more accuracy of using nonlinear regression as against the linear regression used in the original publication which suggests the 2-parameter Jovanovic isotherm as the best model.

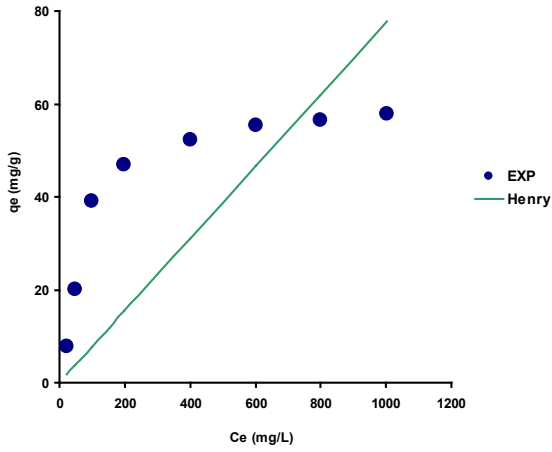


Fig. 1. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Henry model.

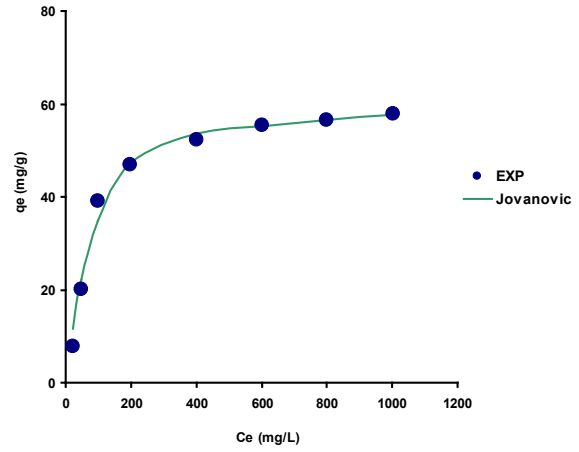


Fig. 4. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Jovanovic isotherm model.

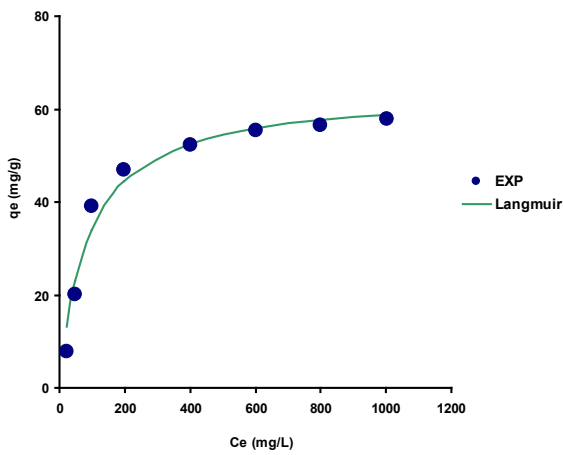


Fig. 2. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Langmuir isotherm model.

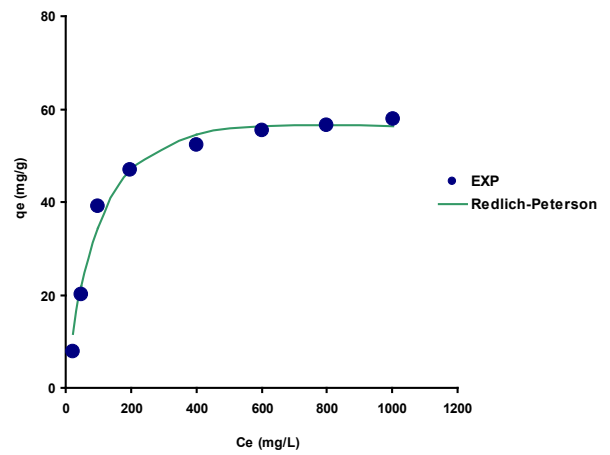


Fig. 5. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Redlich-Peterson isotherm model.

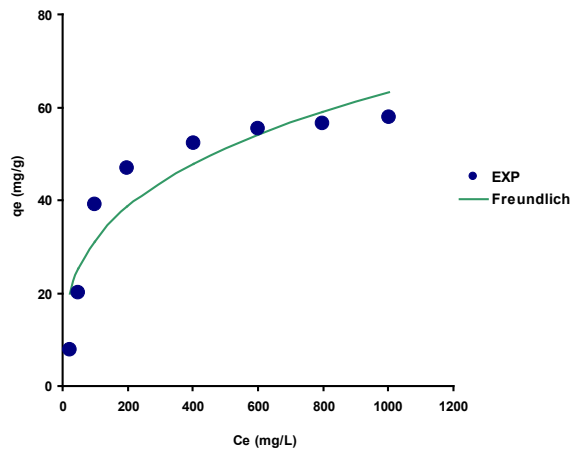


Fig. 3. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Freundlich isotherm model.

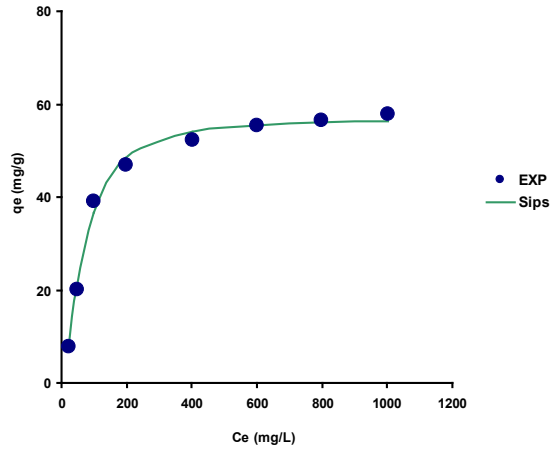


Fig. 6. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Sips isotherm model.

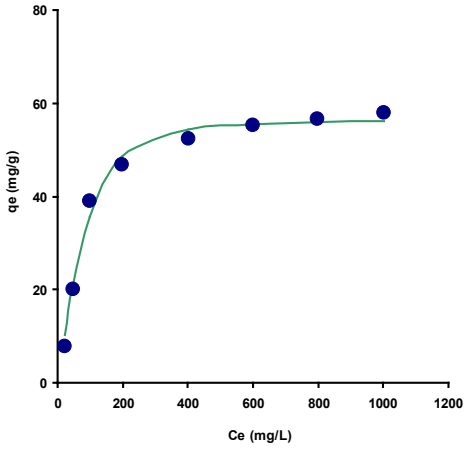


Fig. 7. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Toth isotherm model.

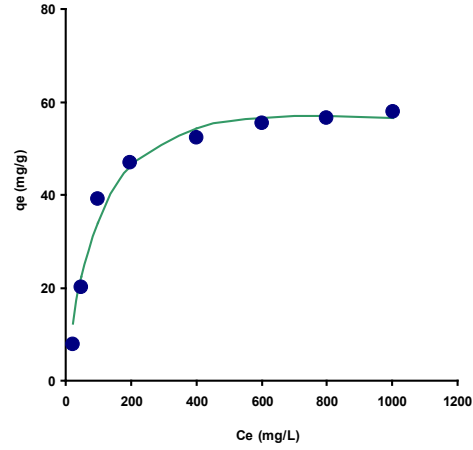


Fig. 10. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the BET isotherm model.

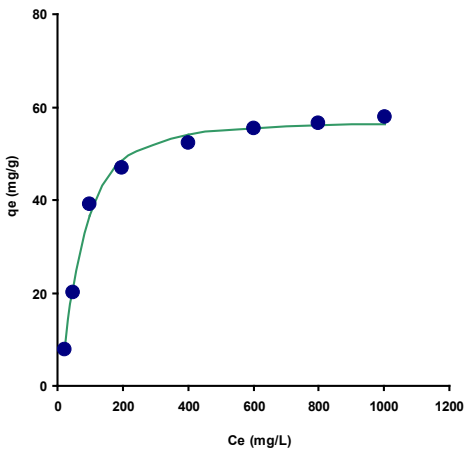


Fig. 8. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Hill isotherm model.

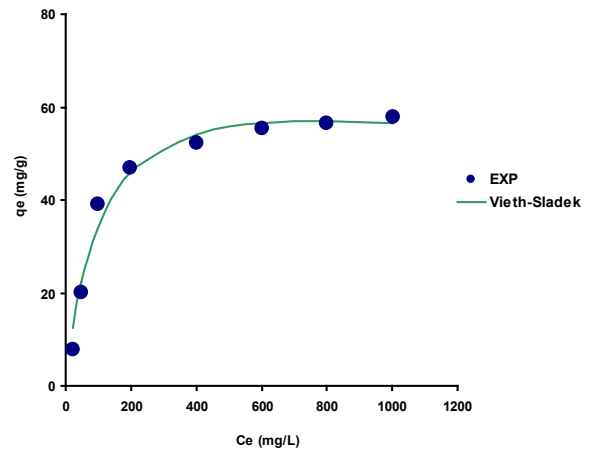


Fig. 11. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Vieth-Sladek isotherm model.

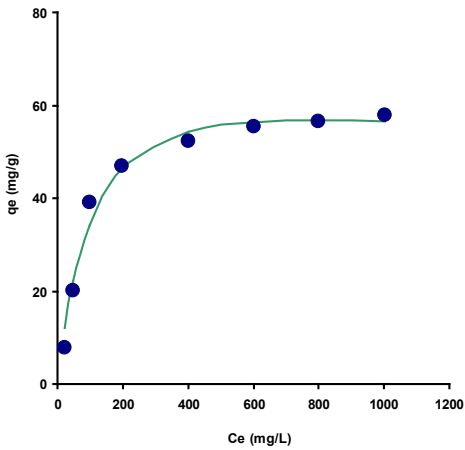


Fig. 9. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Khan isotherm model.

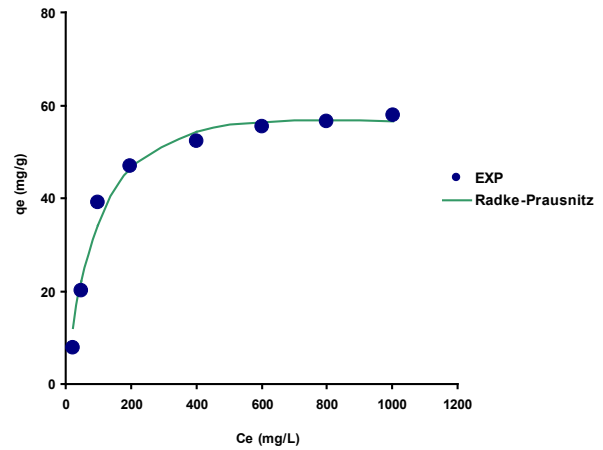
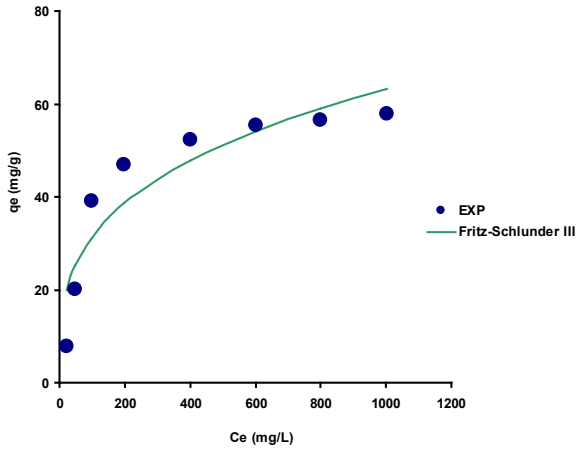
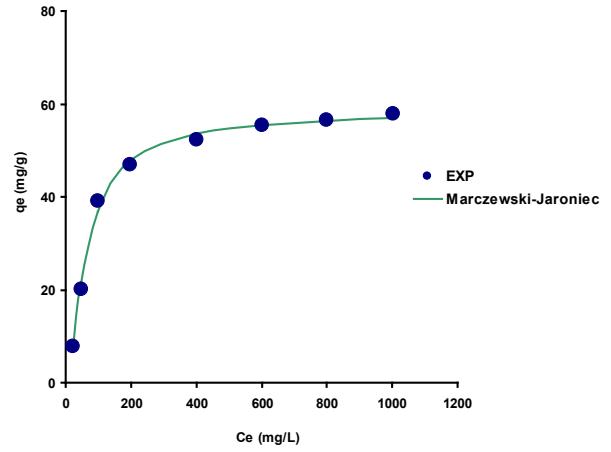


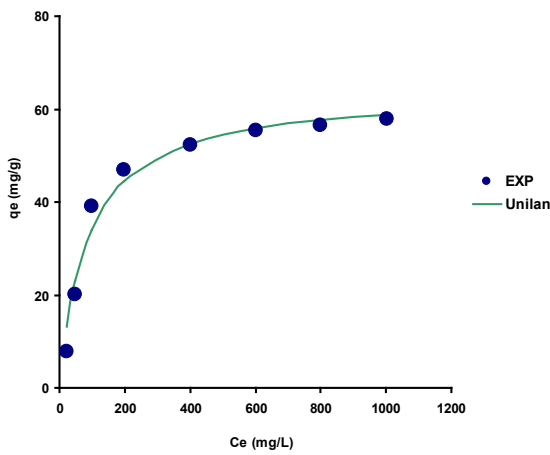
Fig. 12. Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Radke-Prausnitz isotherm model.



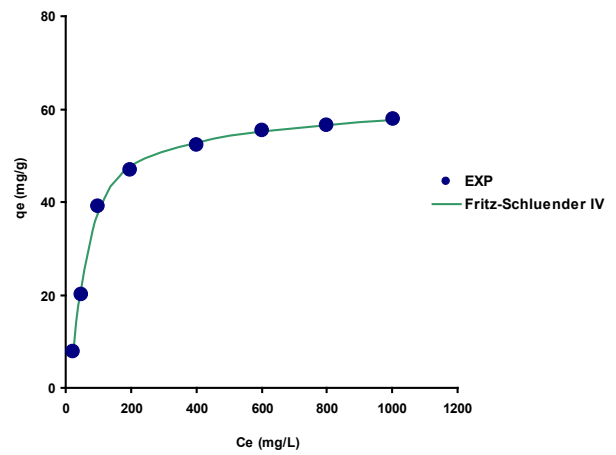
**Fig. 13.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Fritz-Schlunder III isotherm model.



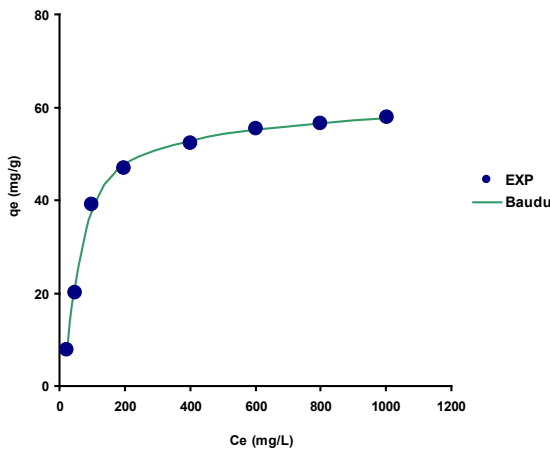
**Fig. 16.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Marczewski-Jaroniec isotherm model.



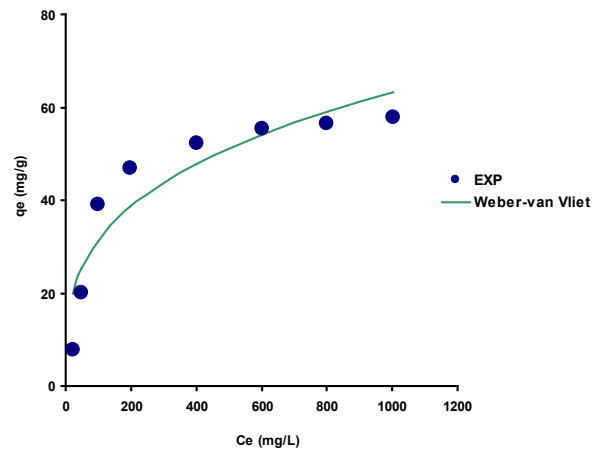
**Fig. 14.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Unilan isotherm model.



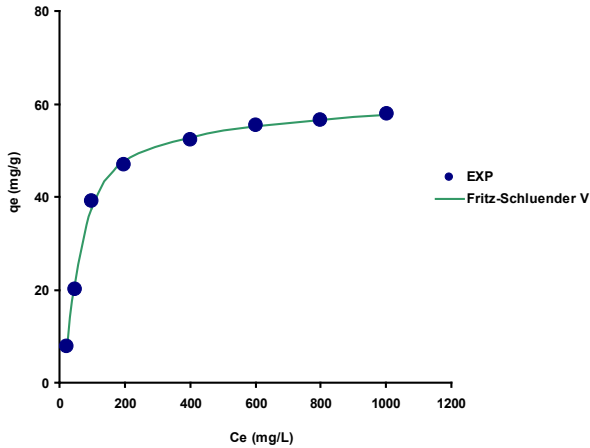
**Fig. 17.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Fritz-Schlunder IV isotherm model.



**Fig. 15.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Baudu isotherm model.



**Fig. 18.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Weber-van Vliet isotherm model.



**Fig. 19.** Adsorption isotherm of crystal violet onto modified charred rice husk as modelled using the Fritz-Schlunder V isotherm model.

**Table 2.** Error function analysis for the fitting of the isotherm of crystal violet onto modified charred rice husk.

| Model                 | <i>p</i> | RMSE   | <i>adjR</i> <sup>2</sup> | AICc   | BIC   | HQC   | BF   | AF   |
|-----------------------|----------|--------|--------------------------|--------|-------|-------|------|------|
| Henry                 | 1        | 21.500 | 0.35                     | 56.42  | 56.4  | 50.1  | 0.53 | 1.89 |
| Langmuir              | 2        | 3.493  | 0.95                     | 33.71  | 33.7  | 21.87 | 0.99 | 1.04 |
| Freundlich            | 2        | 7.765  | 0.72                     | 46.49  | 46.5  | 34.65 | 0.96 | 1.10 |
| Temkin                | 2        | n.a.   | n.a.                     | n.a.   | n.a.  | n.a.  | n.a. | n.a. |
| Dubinini-Radushkevich | 2        | n.a.   | n.a.                     | n.a.   | n.a.  | n.a.  | n.a. | n.a. |
| Jovanovic             | 2        | 2.486  | 0.98                     | 28.27  | 28.3  | 16.43 | 1.00 | 1.03 |
| Redlich-Peterson      | 2        | 2.829  | 0.97                     | 30.34  | 30.3  | 18.5  | 1.00 | 1.04 |
| Sips                  | 3        | 1.705  | 0.99                     | 32.11  | 32.1  | 11.02 | 1.01 | 1.02 |
| Toth                  | 3        | 2.380  | 0.98                     | 37.44  | 37.4  | 16.35 | 1.01 | 1.03 |
| Hill                  | 3        | 1.705  | 0.99                     | 32.11  | 32.1  | 11.02 | 1.01 | 1.02 |
| Khan                  | 3        | 3.276  | 0.92                     | 42.56  | 42.6  | 21.46 | 1.00 | 1.04 |
| BET                   | 3        | 3.437  | 0.95                     | 43.33  | 43.3  | 22.23 | 1.00 | 1.04 |
| Vieth-Sladek          | 3        | 3.476  | 0.95                     | 43.51  | 43.5  | 22.41 | 1.00 | 1.04 |
| Radke-Prausnitz       | 3        | 3.276  | 0.96                     | 42.56  | 42.6  | 21.46 | 1.00 | 1.04 |
| Brouers-Sotolongo     | 3        | n.a.   | n.a.                     | n.a.   | n.a.  | n.a.  | n.a. | n.a. |
| Fritz-Schlunder III   | 3        | 8.506  | 0.65                     | 57.83  | 57.8  | 36.73 | 0.96 | 1.10 |
| Unilan                | 3        | 3.838  | 0.94                     | 45.09  | 45.1  | 24    | 0.99 | 1.04 |
| Baudu                 | 4        | 1.220  | 0.99                     | 45.64  | 45.6  | 5.96  | 1.01 | 1.02 |
| Marczewski-Jaroniec   | 4        | 1.695  | 0.99                     | 50.90  | 50.9  | 11.21 | 1.01 | 1.02 |
| Fritz-Schlunder IV    | 4        | 1.221  | 0.99                     | 45.65  | 45.7  | 5.97  | 1.01 | 1.02 |
| Weber-van Vliet       | 4        | 9.510  | 0.54                     | 78.49  | 78.5  | 38.81 | 0.96 | 1.10 |
| Fritz-Schlunder V     | 5        | 1.410  | 0.99                     | 103.65 | 103.7 | 8.05  | 1.01 | 1.02 |

Note:  
 RMSE Root mean Square Error  
 $adjR^2$  Adjusted Coefficient of determination  
*p* no of parameters  
 AF Accuracy factor  
 BF Bias factor  
 BIC Bayesian Information Criterion  
 AICc Adjusted Akaike Information Criterion  
 HQC Hannan–Quinn information criterion

The Jovanovic isotherm considers an adsorption surface assumption, which is similar to the Langmuir's. A second approximation for localized monolayer adsorption in the absence of lateral interactions corresponds to this scenario. The main distinction between this model and the Langmuir model is that the surface binding vibrations of an adsorbed species are considered [33].

The maximal adsorption capacity in the Jovanovic model, expressed in milligrams per gram (mg/g), is denoted by  $q_{mJ}$  while  $K_J$  is the Jovanovic constant, and the calculated values were 55.979 mg/L (95% confidence interval; 52.556 to 59.403) and 0.010 (95% confidence interval; 0.008 to 0.012), respectively (Table 3). The isotherm additionally considers the surface binding vibrations of the adsorbed species. A 3-parameter Jovanovic isotherm is also available and considers multilayer adsorption [33].

**Table 3.** Isothermal models' constants for the TB dye adsorption using *Pseudomonas* sp. strain MM02.

| Model              | <i>p</i>     | Unit               | Value  | (95% confidence interval) |
|--------------------|--------------|--------------------|--------|---------------------------|
| Langmuir           | $q_{mL}$     | mg g <sup>-1</sup> | 63.889 | 57.055 to 70.723          |
|                    | $b_L$        | L mg <sup>-1</sup> | 0.012  | 0.006 to 0.017            |
| Jovanovic          | $q_{mJ}$     | mg g <sup>-1</sup> | 55.979 | 52.556 to 59.403          |
|                    | $K_J$        | dimensionless      | 0.010  | 0.008 to 0.012            |
| Redlich – Peterson | $K_{RP}$     | L mg <sup>-1</sup> | 0.003  | -0.004 to 0.011           |
|                    | $i$          | dimensionless      | 1.147  | 0.875 to 1.419            |
|                    | $\beta_{RP}$ | L g <sup>-1</sup>  | 0.577  | 0.297 to 0.856            |
| Sips               | $z$          |                    |        |                           |
|                    | $q_{mS}$     | mg g <sup>-1</sup> | 57.089 | 54.037 to 60.140          |
|                    | $K_S$        | L g <sup>-1</sup>  | 0.001  | -0.001 to 0.003           |
| Hill isotherm      | $n_S$        | dimensionless      | 0.613  | 0.462 to 0.765            |
|                    | $q_{mH}$     | mg g <sup>-1</sup> | 57.089 | 54.037 to 60.140          |
|                    | $n_H$        | dimensionless      | 1.63   | 1.228 to 2.033            |
|                    | $K_H$        | dimensionless      | 980.2  | -617.9 to 2578.3          |

Note  
 \*Isotherm with  $\ln$  term should not be plotted using data that starts from the origin (0,0)  
 †Isotherms having an RT term should be plotted using the temperature (Kelvin) studied

Dye, effluent, and trace element removal from wastewater can be accomplished using a variety of sorbents prepared by coating, chemical synthesis, and other methods [46–51]. Rice husk is a waste product created during the milling of rice. In terms of total volume, it is among the most significant agricultural byproducts. It's responsible for about 20% of the total rice output in some nations, including Egypt [52,53]. It is estimated that developing countries would produce 500 million tons of rice each year, with around 100 million tons of rice husk available for utilization. Historically, rice husks have been employed not only by the rice industry as a fuel source for boilers, but also in the production of blocks used in civil construction as panels [53,54]. However, there are many more rice husks available that can be used locally, leading to disposal problems. The granular structure, chemical stability, and inexpensive production costs of this material led to its selection, as did the fact that it does not require regeneration.

## CONCLUSION

Finally, multiple models with one to five parameters have been fitted using non-linear regression to the adsorption isotherm data of crystal violet dye onto modified charred rice husk. Root-mean-square error (RMSE), adjusted coefficient of determination ( $adjR^2$ ), bias factor (BF), accuracy factor (AF), bias information coefficient (BIC), and the corrected Akaike Information Criterion (AICc) all indicate that the showed that the Fritz-Schlunder IV model was the best model in terms of overall best criteria. The maximal adsorption capacity in the Jovanovic model, expressed in milligrams per gram (mg/g), is denoted by  $q_{mJ}$  while  $K_J$  is the Jovanovic constant, and the calculated values were 55.979 mg/L (95% confidence interval; 52.556 to 59.403) and 0.010 (95% confidence interval; 0.008 to 0.012), respectively. The nonlinear regression approach represents parameter values in the 95% confidence interval range, which allows for better comparison with published findings.

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