INTRODUCTION

Rubber exports brought in between one and two billion dollars a year for Malaysia. Even while the expansion of the rubber goods manufacturing sector in Malaysia has been good for the country's economy, the industry's heavy water consumption and the environmental harm it has caused are two sides of the same coin. Malaysia's economy has benefited from the growth of the rubber goods manufacturing industry [1–3]. It is stated that the manufacture of rubber thread contributes the most to the pollution problem among the industries dealing with rubber goods. The main concern is the alarmingly high concentration of zinc in the effluent. About 135 organizations fall within this category (latex products, tires and tubes, industrial and general rubber goods, and footwear). The wastewater produced by these companies has a high concentration of organic waste, as measured by the chemical oxygen demand (COD) and biological oxygen demand (BOD). The abundance of organic debris in the sewer water lends credence to these conclusions [4–7]. The department of environment in Malaysia has defined guidelines for the pH of wastewater, and this value is significantly lower than the permissible value range.

Furthermore, it was found that the levels of pollutants in this wastewater were the highest compared to the levels of contaminants found in wastewater from facilities producing other types of rubber goods. Many different methods, such as activated sludge or anaerobic digestion, aerated lagoons, anaerobic/facultative ponding, and so on, are used in the last stage of wastewater treatment in the rubber products manufacturing business. Flocculation is a common step in the pretreatment process for removing zinc from wastewater but is
expected to become an expensive method in the years to come [8–12]. Some of the new and improved treatment procedures that have been developed as a result of this issue are currently making their way to facilities of this type. Many various treatment processes have been proposed in the literature as viable options for extracting heavy metals including zinc from water supplies. These include coagulation, chemical precipitation, evaporation, electrolysis, adsorption, and reverse osmosis. However, these older forms of technology may not be enough, may be too costly, or may introduce new complications. Therefore, adsorption is likely the most appealing of these approaches since it is easy to apply and competitive and effective [13–19]. But the cost of the adsorbent and the energy needed for its replenishment might act as a roadblock to future progress.

The reuse and/or recycling of garbage and other similar materials is becoming an increasingly important topic, and there is a corresponding increase in interest in the use of inexpensive materials for adsorptive uses. One area where this is becoming increasingly important is in the field of adsorptive materials, where both the need for and demand in inexpensive options is expanding. Several recent studies have described research that makes use of adsorbents such rice husk and ash, which are cheap and readily available in the area where the research was conducted [20–24].

Biosorption is a method for decontaminating dirty water that does not involve any danger and is very cost effective. Biosorbents may be made from either biomass or natural substrates. In recent years, a great deal of research on mercury biosorption that is of a high quality and was conducted at a reasonable cost has been published. Adsorbents that can be acquired in vast numbers with little to no effort, that are prevalent in the natural world, or that are by-products of industrial processes are examples of low-cost adsorbents. Rice husk may be used as a fuel to create steam, which allows a variety of enterprises to cut their costs for both energy and materials. Rice husk ash is the ash that is left over after burning rice husk and is collected in a dust collector that is positioned upstream from the stacks of rice husk-fired boilers and furnaces. This gives the ash its name (RHA). RHA has been utilized in the past to successfully do this task because to the powerful adsorption qualities that it possesses [20–24].

It is absolutely necessary to have an accurate assignment of the kinetics and isotherms of the biosorption process in order to have an adequate understanding of the biosorption process in these species. A linearized form of what is plainly a nonlinear curve of these data is commonly reported in the scientific literature. When nonlinear data is linearized, the error structure of the data is changed. This makes it more difficult to quantify uncertainty, which is sometimes portrayed as a confidence range of 95 percent. The aim of this work is to remodel a published work on Zn sorption to rice husk ash [25], which utilize linear regression to obtain best fitting models.

METHOD

Data acquisition and fitting

Figure 2 data from a previously published study [25] was digitized using the freeware Webplotdigitizer 2.5 [26]. After that, the data were nonlinearly regressed using the curve-fitting program Curve-Expert Professional (Version 2.6.5, copyright Daniel Hyams). Implicit equations were solved using MATLAB (Mathworks, Massachusetts, United States). Digitization using this program has been praised for its dependability [27].

Isotherms

As the value of the datapoints is very small, only models having parameters of up to three were considered to prevent overfitting.

Table 1. Mathematical models that were used in modelling data [28,29].

<table>
<thead>
<tr>
<th>Isotherm</th>
<th>p</th>
<th>Formula</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Henry’s law</td>
<td>1</td>
<td>( q_e = \frac{K_a}{b + C_e} )</td>
<td>[30]</td>
</tr>
<tr>
<td>Langmuir</td>
<td>2</td>
<td>( q_e = \frac{q_m b C_e}{1 + b C_e} )</td>
<td>[28]</td>
</tr>
<tr>
<td>Jovanovic</td>
<td>2</td>
<td>( q_e = \frac{q_m (1 - e^{-C_e / C})}{1 + b C_e} )</td>
<td>[31]</td>
</tr>
<tr>
<td>Freundlich</td>
<td>2</td>
<td>( q_e = K_f \frac{C_e}{1 + b C_e} )</td>
<td>[32]</td>
</tr>
<tr>
<td>Dubinin-Radushkevitch</td>
<td>2</td>
<td>( q_e = K_0 \rho_0 \exp \left( -\frac{R T \ln \left( 1 + \frac{1}{C_e} \right)}{\alpha} \right) )</td>
<td>[33,34]</td>
</tr>
<tr>
<td>Temkin</td>
<td>3</td>
<td>( q_e = \frac{R T}{b_T} \left( \ln \left( c_T \right) \right) )</td>
<td>[35,36]</td>
</tr>
<tr>
<td>Redlich-Peterson</td>
<td>3</td>
<td>( q_e = \frac{K_a C_e}{1 + K_a C_e} )</td>
<td>[37]</td>
</tr>
<tr>
<td>Sips</td>
<td>3</td>
<td>( q_e = \frac{K_a C_e}{1 + K_a C_e} )</td>
<td>[38]</td>
</tr>
<tr>
<td>Toth</td>
<td>3</td>
<td>( q_e = \frac{K_a C_e}{1 + K_a C_e} )</td>
<td>[39]</td>
</tr>
<tr>
<td>Hill</td>
<td>3</td>
<td>( q_e = K_a C_e )</td>
<td>[40]</td>
</tr>
<tr>
<td>Khan</td>
<td>3</td>
<td>( q_e = \frac{(1 + b C_e) C_e}{\rho_0 \alpha + b C_e} )</td>
<td>[41]</td>
</tr>
<tr>
<td>BET</td>
<td>3</td>
<td>( q_e = \frac{(1 - \beta_{2 \alpha} C_e) (1 - \beta_{2 \alpha} C_e + \alpha_{2 \alpha} C_e)}{q_{max} (1 - \beta_{2 \alpha} C_e + \alpha_{2 \alpha} C_e)} )</td>
<td>[42]</td>
</tr>
<tr>
<td>Vieth-Sladek</td>
<td>3</td>
<td>( q_e = \frac{K_{d,1} C_e^a}{1 + b_{12} C_e^{b_{12}}} )</td>
<td>[43]</td>
</tr>
<tr>
<td>Radke-Prausnitz</td>
<td>3</td>
<td>( q_e = \frac{(1 + K_a C_e) \rho_0 \alpha}{K_a C_e} )</td>
<td>[44]</td>
</tr>
<tr>
<td>Brouers-Sotolongo</td>
<td>3</td>
<td>( q_e = q_{max} \left( 1 - \exp \left( -K_a C_e \right) \right) )</td>
<td>[45]</td>
</tr>
<tr>
<td>Fritz-Schlunder-III</td>
<td>3</td>
<td>( q_e = \frac{q_{max} K_a C_e}{1 + K_a C_e} )</td>
<td>[46]</td>
</tr>
<tr>
<td>Fowler-Guggenheim*</td>
<td>3</td>
<td>( q_e = q_{max} \left( 1 + K_a C_e \right) )</td>
<td>[47]</td>
</tr>
<tr>
<td>Moreau</td>
<td>3</td>
<td>( q_e = \frac{q_{max} A_n}{1 + b C_e} )</td>
<td>[48]</td>
</tr>
<tr>
<td>Unilan</td>
<td>3</td>
<td>( q_e = \frac{q_{max} A_n \ln \left( \frac{A_n + C_e}{A_n + C_e^2} \right)}{2 b \ln \left( \frac{A_n + C_e}{A_n + C_e^2} \right)} )</td>
<td>[28]</td>
</tr>
</tbody>
</table>

Note *Implicit equation or function.

Statistical analysis

A set of statistical discriminatory tests were utilized to find the best model and are as follows;

The RMSE was computed using Equation 1, and it stands to reason that the fewer parameters utilized, the smaller the RMSE will be. n is for the total number of observations made in the experiment, Obi and Pdi stand for the total number of observations made in the experiment and projections, and p stands for the total number of parameters [49].

\[
RMSE = \left( \frac{\sum_{i=1}^{n} (P_{di} - Ob_i)^2}{n-p} \right)^{1/2} \quad (\text{Eqn. 1})
\]

Because \( R^2 \) or the coefficient of determination ignores the number of parameters in a model, the modified \( R^2 \) is used to overcome this limitation. The entire variance of the \( y \)-variable is given by \( S_y^2 \) in the equation (Equations 2 and 3), while RMS is the Residual Mean Square.

\[
\text{Bias factor} = 10 \left( \frac{\sum_{i=1}^{n} \log \left( \frac{P_{di}}{Ob_i} \right)}{n} \right) \quad (\text{Eqn. 2})
\]
Accuracy factor = \( 10 \left( \sum_{i=1}^{n} \log \left( \frac{(Pd_i/Ob_i)}{n} \right) \right) \)  \( \text{(Eqn. 3)} \)

The AICc is computed as follows (Equation 4), where \( p \) represents the number of parameters and \( n \) represents the number of data points. The corrected Akaike information criterion (AICc) is used to manage data with a large number of parameters but a limited number of values [50]. A model with a lower AICc score is considered more likely to be right [50]. The information theory is the foundation of the Akaike Information Criterion (AIC). It strikes a compromise between the goodness of fit of a given model and the model's complexity [51].

\[
AICc = 2p + n \ln \left( \frac{RSS}{n} \right) + \frac{2p+1+2(p+2)}{n-p-2} \text{ } \text{(Eqn. 4)}
\]

Another statistical tool based on information theory apart from AICc, is the Bayesian Information Criterion (BIC) (Equation 5). The number of parameters is penalized more severely by this error function than by AIC [26].

\[
BIC = n \ln \left( \frac{RSS}{n} \right) + k \ln(n) \text{ } \text{(Eqn. 5)}
\]

The Hannan-Quinn information criterion (HQC) (Equation 6) is another error function approach based on information theory. Because of the \( \ln \ln n \) element in the calculation, the HQC is more consistent than the AIC [50].

\[
HQC = n \ln \left( \frac{RSS}{n} \right) + 2k \ln(\ln n) \text{ } \text{(Eqn. 6)}
\]

The Accuracy Factor (AF) and Bias Factor (BF) are two further error function analyses derived from Ross’s work [50]. These error functions evaluate models statistically for goodness-of-fit but do not penalize for the number of parameters (Equations 7 and 8).

\[
Adjusted \ (R^2) = 1 - \frac{RSS}{S^2} \text{ } \text{(Eqn. 7)}
\]

\[
Adjusted \ (R^2) = 1 - \frac{(1-R^2)(n-1)}{(n-p-1)} \text{ } \text{(Eqn. 8)}
\]

Marquardt’s percent standard deviation (MPSD) is another penalty-imposed error function that has been extensively utilized in numerous isotherm studies. The function has some similarity to a geometric mean error distribution that is altered according to the system’s number of degrees of freedom [52]. Among the first to use this error function in the adsorption field is [53] and the error function’s official term that is known as MPSD (Equation 9) was introduced by the McKay group [54].

\[
MPSD = 100 \sqrt{ \frac{1}{n-p} \sum_{i=1}^{n} \left( \frac{Ob_i-Pd_i}{Ob_i} \right)^2 } \text{ } \text{(Eqn. 9)}
\]

where \( n \) is the number of experimental data, \( p \) is the number of parameters, \( Ob_i \) is the experimental data, and \( Pd_i \) is the value predicted by the model.

**RESULTS AND DISCUSSION**

The equilibrium data from [55] was analyzed using the models—Henry, Langmuir, Freundlich, Redlich-Peterson, Sips, BET, Toth, Hill, Khan, Vieth-Slake, Radke-Prausnitz, Unilan, Fritz-Schlunder III, Fritz-Schlunder IV, and Fritz-Schlunder V, were used in finding the best fit by utilizing non-linear regression. Henry, Langmuir, Hill, Vieth-Slake, Unilan, Sips and BET does not fit well with the data, whereas Freundlich, Redlich-Peterson, Toth, Khan, Radke-Prausnitz, Fritz-Schlunder III, Fritz-Schlunder IV, and Fritz-Schlunder V, fitted well with the data (Figs. 1 – 19). The best isotherm model was found to be the Freundlich with the best combination of low values for AICc, BIC, HQC and RMSE and values of AF, BF and adj\( R^2 \) values closest to unity. This is followed (descending order) by Langmuir and Jovanovic as the next top three best model (Table 2). As enough models fitted well with the charred rice husk data, it explains and justifies the more accuracy of using nonlinear regression as against the linear regression used in the original publication which suggests the 2-parameter Jovanovic isotherm as the best model.
Fig. 3. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Freundlich isotherm model.

Fig. 4. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Temkin isotherm model.

Fig. 5. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Dubinin-Radushkevich isotherm model.

Fig. 6. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Jovanovic isotherm model.

Fig. 7. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Redlich-Peterson isotherm model.

Fig. 8. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Sips isotherm model.
Fig. 9. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Toth isotherm model.

Fig. 10. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Hill isotherm model.

Fig. 11. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Khan isotherm model.

Fig. 12. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the BET isotherm model.

Fig. 13. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Vieth-Sladek isotherm model.

Fig. 14. Adsorption isotherm of Zn (II) onto rice husk ash as modelled using the Radke-Prausnitz isotherm model.
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Langmuir isotherm

The Langmuir isotherm is one of several isotherm models that are mechanistic rather than empirical. The model envisioned adsorbate being adsorbed onto the adsorbent in a single, uniform layer. For monolayer adsorption to take place, the isotherm assumes that all adsorption sites have the same energy and that the adsorbent is structurally homogenous [56]. Due to the exponential reduction of intermolecular interactions with increasing distance, this isotherm model predicts the occurrence of monolayer coverage of the adsorbent at the outer surface of the adsorbent. In addition to simplifying the linear relationship, this model predicts a constant monolayer adsorption capacity. The model also predicts that the Henry's model become valid for both very dilute and very concentrated solute concentrations [57].

The Langmuir, together with the Freundlich model are amongst the most utilized models and appear in nearly all sorption works. The maximum adsorption parameter and the model constant predicted using the nonlinear regression approach was nearly the same to the original study but could not provide the 95% confidence interval for the estimated parameters. The value of the maximum monolayer adsorption capacity for Zn binding to rice husk ash according to the Langmuir’s parameter \( q_{\text{ml}} \) was 7.33 mg g\(^{-1}\) (95% Confidence interval from5.464 to 9.187), while \( b_L \) (L mg\(^{-1}\)), the Langmuir model constants was 0.011 L mg\(^{-1}\) (95% C.I. from 0.030 to 0.182). These values are much lower than the reported linear regressed values in the original publication [25]. Literature search showed that biosorption of Zinc (II) using microbial and plant-based adsorbents exhibits a maximum adsorption capacity of between 5 and 50 mg g\(^{-1}\) (Table 3), which is a typical result.

Freundlich isotherm

One common empirical model for adsorption and desorption is the Freundlich equation, which was first derived for the gas phase. The adsorbate creates a monomolecular layer on the adsorbent’s surface in a Freundlich adsorption isotherm. While the Freundlich equation does give some useful empirical data on particle sorption, its applicability is limited at a particular concentration, at which point it becomes nonlinear [58–60]. Unlike the Langmuir isotherm, the Freundlich model can be generalized to multilayer adsorption. This isotherm model allows for a heterogeneous surface to have a variable distribution of adsorption heat and affinities. The model also proposed an exponential distribution of the active sites and energy for adsorbate binding and also presumes surface heterogeneity. The Freundlich isotherm model was first used to describe the adsorption of an adsorbate onto charcoal.

The mass ratio of the adsorbate onto the adsorbent changed as the concentration of the solution changed. This means that the sum of the adsorption at each site is equal to the adsorbed amount. Once the most stable binding sites are occupied, the adsorption energy drops at an exponential rate [57,61,62]. The Freundlich model was also the best model for Zn sorption to Streptomyces sp. [19], leaves of Corchorus olitorius [63], activated carbon/silica compo-site [64] and to coffee waste [65] (Table 3).

In other examples, the Freundlich model was also the best model for lead(II) sorption by a modified Jordanian zeolite [66], by a Guar gum/bentonite biocomposite [67], Chlorococcum aquaticum biomass [68] and nanoparticle adsorbents of cellulose origin [69] and the sorption of other metal and radionuclides [70–75].

Because of its empirical nature, the Freundlich model is unable to forecast the maximal adsorption capacity in which \( K_F \) (mg g\(^{-1}\cdotL \text{ mg}^{-1})^{1/n_F} \) is the Freundlich isotherm constant, and \( n_F \) is the Freundlich exponent. A small 1/\( n_F \) value indicates a heterogeneous system [58,76]. Since there is only a single KF term in the Freundlich equation, this shows that the adsorption energy on a homogeneous surface is unaffected by the quantity of surface coverage. Various slopes in Freundlich isotherms are often seen as evidence of multiple binding sites, and researchers have drawn many inferences regarding adsorption processes based on the KF and 1/nF parameters. These inferences, however, are very speculative, and the KF and 1/nF parameters should not be used as a basis for them [77]. As the Freundlich equation is unable to model the maximum adsorption, the Halsey rearrangement of the Freundlich equation [78] (Equation 10) gave the estimated maximum absorption of 7.20 mg g\(^{-1}\), which is very close to the experimental value.

\[
K_F = \frac{n_F}{c_0^{1/n_F}} \quad \text{(Eqn. 10)}
\]

Jovanovic isotherm

The Jovanovic isotherm is similar to the Langmuir in that it takes into account an adsorption surface assumption. In this case, we can use a second approximation for monolayer adsorption that accounts for the lack of lateral interactions. The surface binding vibrations of an adsorbed species are taken into account, which is the main difference between this model and the Langmuir model [31]. The isotherm also takes into account the adsorbed species' surface binding vibrations. Multilayer adsorption can also be accounted for with the help of a 3-parameter Jovanovic isotherm [31].

Table 3. Summary of recent Zn (II) sorption studies.

<table>
<thead>
<tr>
<th>Adsorbent</th>
<th>Kinetics</th>
<th>Isotherm</th>
<th>Linear or Nonlinear Regression</th>
<th>Experimental uptake, ( Q_e ) (mg/g)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Streptomyces sp.</td>
<td>PSO</td>
<td>Freundlich</td>
<td>L</td>
<td>4.65</td>
<td>[19]</td>
</tr>
<tr>
<td>Saccharomyces cerevisiae</td>
<td>PSO</td>
<td>Freundlich</td>
<td>L</td>
<td>20.38</td>
<td>[79]</td>
</tr>
<tr>
<td>Sargassum polycystum</td>
<td>PSO</td>
<td>Langmuir</td>
<td>NL</td>
<td>116.2</td>
<td>[80]</td>
</tr>
<tr>
<td>Alium Cepa seed biomass</td>
<td>PSO</td>
<td>Langmuir</td>
<td>NL</td>
<td>1.68</td>
<td>[81]</td>
</tr>
<tr>
<td>alginate extraction process</td>
<td>PSO</td>
<td>Langmuir</td>
<td>NL</td>
<td>51.06</td>
<td>[14]</td>
</tr>
<tr>
<td>waste leaves of Corchorus</td>
<td>n.a.</td>
<td>Freundlich</td>
<td>L</td>
<td>11.63</td>
<td>[63]</td>
</tr>
<tr>
<td>olitorius</td>
<td></td>
<td></td>
<td>(Langmuir)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sulphuric acid treated</td>
<td>PSO</td>
<td>Langmuir</td>
<td>L</td>
<td>1.292</td>
<td>[82]</td>
</tr>
<tr>
<td>sugarcane bagasse</td>
<td></td>
<td></td>
<td>(Langmuir)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Activated carbon/silica</td>
<td>n.a.</td>
<td>Freundlich</td>
<td>L</td>
<td>344.82</td>
<td>[64]</td>
</tr>
<tr>
<td>composite</td>
<td></td>
<td></td>
<td>(Langmuir)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NaOH-treated rice husk</td>
<td>PSO</td>
<td>Langmuir</td>
<td>L</td>
<td>20.08</td>
<td>[83]</td>
</tr>
<tr>
<td>Scedesmus sp. MCC 26</td>
<td>n.a.</td>
<td>Freundlich</td>
<td>L</td>
<td>142.85</td>
<td>[84]</td>
</tr>
<tr>
<td>Coffee waste</td>
<td>n.a.</td>
<td>Freundlich</td>
<td>L</td>
<td>46.05</td>
<td>[65]</td>
</tr>
<tr>
<td>oil palm waste ash particles</td>
<td>PFO</td>
<td>Langmuir</td>
<td>NL</td>
<td>10.655</td>
<td>[85]</td>
</tr>
</tbody>
</table>

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Metal removal from wastewater can be accomplished using a variety of sorbents prepared by coating, chemical synthesis, and other methods [18, 86–97]. Rice husk is a waste product created during the milling of rice. In terms of total volume, it is among the most significant agricultural byproducts. It's responsible for about 20% of the total rice output in some nations [98, 99]. It is estimated that developing countries would produce 500 million tons of rice each year, with around 100 million tons of rice husk available for utilization. Historically, rice husks have been employed not only by the rice industry as a fuel source for boilers, but also in the production of blocks used in civil construction as panels [99, 100]. However, there are many more rice husks available that can be used locally, leading to disposal problems. The granular structure, chemical stability, and inexpensive production costs of this material led to its selection, as did the fact that it does not require regeneration.

**CONCLUSION**

Finally, multiple models with one to three parameters have been fitted using non-linear regression to the adsorption isotherm data of Zn (II) dye onto rice husk ash. Root-mean-square error (RMSE), adjusted coefficient of determination (adjR2), bias factor (BF), accuracy factor (AF), bias information coefficient (BIC), and the corrected Akaike Information Criterion (AICc) all indicate that the showed that the Freundlich model was the best model in terms of overall best criteria. The Freundlich model is unable to forecast the maximal adsorption capacity. The Halsey rearrangement of the Freundlich equation gave the estimated maximum absorption capacity for Zn binding to rice husk ash according to the experimental value. The value of the maximum monolayer adsorption capacity for Zn binding to rice husk ash according to the Langmuir parameter qm, was 7.33 mg g⁻¹ (95% Confidence interval from 0.464 to 9.187), while bc = L mg⁻¹, the Langmuir model constant was 0.011 L mg⁻¹ (95% C.I. from 0.303 to 0.182). These values are much lower than the reported linear regressed values in the original publication. The nonlinear regression approach represents parameter values in the 95% confidence interval range, which allows for better comparison with published findings.

**REFERENCE**


