

## Substrate Inhibition Kinetics Models for Fitting the Growth Rate of Phenol by an Acclimatized Mixed Bacterial Consortia from an Anaerobic Batch Reactor

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### ABSTRACT

Particularly hazardous among the numerous synthetic chemicals made by mankind is phenol. A considerable number of the over 80,000 chemicals manufactured in the United States for industrial purposes are phenol and phenolic compounds, which enter the environment without undergoing sufficient safety evaluation. The potential utilization of phenol as a carbon source by several species of bacteria renders bioremediation of this hazardous substance an auspicious prospect. Our research revealed that the growth rate of acclimatized mixed bacterial consortia from an anaerobic batch reactor was considerably inhibited when exposed to extremely high quantities of phenol. The growth parameter-specific growth rate was determined by employing the modified Gompertz primary growth model. In the present investigation, we extend our previous work by employing multiple substrate inhibition kinetic models—including Monod, Teissier, Haldane, Yano and Koga, Aiba, Han and Levenspiel, Luong, Moser, Webb, and Hinshelwood—to further model the effect of substrate or phenol on the growth rate of the bacterium. All cases exhibit significant fits, with the exception of the Luong and Hinshelwood models. The Haldane model exhibited a higher degree of correspondence with the growth rate data obtained at various concentrations of phenol, as determined by the statistical tests. The designated values of the Haldane constants were maximal reduction rate, half saturation constant for maximal reduction and half inhibition constant which are symbolized by  $\mu_{max}$ ,  $K_s$  and  $K_i$  were 0.157 hr<sup>-1</sup> (95% confidence interval 0.072 to 0.231), 32.042 mg/L (95% C.I. 14.603 to 49.480) and 234.095 mg/L (95% C.I. 181.83 to 286.17), respectively. The output of curve fitting interpolation should not be considered the true value, and the user should be duly informed of this as the true  $\mu_{max}$  should be the point at which the slope's gradient becomes zero; in this instance, the value was 0.095 h<sup>-1</sup> at 50.1 mg/L phenol.

### INTRODUCTION

Synthetic chemicals created by humans, in particular, pose significant dangers to human health. Well over 80,000 chemicals were produced in the United States for use in industry, and many more compounds than that were discharged into the atmosphere

without first undergoing enough testing to ensure their safety. Although it is correct that the toxicity of natural compounds and created chemicals cannot be compared, it is noteworthy to note that the five substances that are considered to be the most hazardous on Earth are all naturally occurring [1]. The phenol industrial pollutant is one of the most prevalent potentially

harmful compounds that are a direct result of the process of industrialization [2]. Phenol pollution of soils and water bodies has increased throughout the years, leading in worry for its removal from the environment.[3].

The acute symptoms of phenol poisoning can be caused by inhaling phenol or coming into direct contact with it through the skin. Phenol is known to be particularly irritating to the eyes, skin, and mucous membranes. A fast heartbeat, difficulty breathing, loss of coordination and tremor, fainting, and coma are some of the indications of intoxications in humans. Acute poisoning in humans can manifest itself in a variety of ways, including abnormal breathing patterns, trembling and weakening of the muscles, loss of balance, seizures, coma, and respiratory arrest. It has been observed that rodents, such as rats, mice, and rabbits, suffer from high levels of acute toxicity as a result of oral exposure to phenol [4–7].

A lack of energy, progressive weight loss, nausea, vertigo, excessive salivation, and a dark urine coloration are some of the chronic effects of phenol exposure in humans. In addition, impacts on the blood and liver, and also problems in the digestive system, have been observed. According to the findings of one research, after a subject was exposed to phenol by inhalation and skin contact, the subject experienced muscle pain and weakness, along with an enlarged liver and increased levels of liver enzymes. The use of phenol topically results in irritation and necrosis of the dermis. Arrhythmias in the heart have been observed in humans who were subjected to extraordinarily high amounts of phenol. When animals inhale phenol for extended periods of time, it has a toxic effect on their kidneys, central nervous system (CNS), liver, and lungs, and it can even affect their hearts.

The Reference Dose for phenol was determined to be 0.6 mg/kg/day after research on rats showed that fetal body weights were reduced. The reference dose is an oral exposure assessment for the public at large (as well as sensitive subgroups) which is anticipated to present no significant risk of adverse noncancerous outcomes over the course of a lifetime. This is the case because the reference dose is below the level at which cancer can develop. It is not an accurate measurement of risk; rather, it is a standard by which to judge the results. When exposures are higher than the reference dosage, there is a greater possibility that negative health outcomes will develop. A lifetime of contact in excess of the reference dosage does not necessarily result in the absence of detrimental effects on one's health in all cases. The EPA has low confidence in the study that was used to derive the reference dose because the dose was given via gavage in that study. But nevertheless, the data includes several supplementary studies (chronic, subchronic and reproductive/developmental), so the EPA has medium confidence in the reference dose overall [4,8–12].

Workers who were exposed to phenol reported slight increases in the likelihood of acquiring certain cancers; nevertheless, a connection between their phenol exposure and their higher cancer risk could not be established. However, dermal treatment of phenol may increase tumor growth and/or be a mild skin carcinogen in mice. Oral dosing of phenol did not cause malignancies in animals; however, dermal application of phenol did. In spite of this, the Environmental Protection Agency has classified phenol as "not classifiable as to human carcinogenicity" in Group D due to the paucity of knowledge regarding its carcinogenic effects in both humans and animals [13].

The biological method is the most popular treatment technology for phenol-containing wastewater around the world at the moment, and it has garnered a lot of attention as a result. In comparison to the physicochemical methods, the biological method has several advantages, including a straightforward pre-treatment process, a low initial investment in equipment, a high treatment capacity, the ability to be sustainable, and the absence of secondary pollution. Therefore, it is essential for the long-term growth of the environmental protection sector to conduct research on the methods of bioremediation for phenolic wastewater by microorganisms. To this day, a great number of bacteria capable of digesting phenol have been found [14–21].

Without accessibility to quantitative experimental data, it is not possible to build biological transformation processes and then optimize those processes. Several various mathematical models have been proposed in order to explain the metabolic characteristics of compounds when those chemicals are exposed to either pure cultures of microorganisms or wild populations of microorganisms. The relationship between the substrate concentration (S) and the specific growth rate ( $\mu_{max}$ ) of a microbial colony is an important tool in biotechnology. The Monod equation is a typical tool that is used to characterize the relationship between growth and the rate of substrate consumption [22,23]. When a substrate, on the other hand, acts as an inhibitor of its own biodegradation, the original Monod model is rendered completely useless. In its place, the development of novel constant-carrying derivatives has taken place in order to facilitate substrate-related changes. The Haldane model is one that is used to represent substrate inhibition of growth or degradation rate, and it may be found in a wide variety of published works. Even though it has been demonstrated that alternative models are more accurate when taking into account a large number of substrate-inhibiting compounds all at once, such as phenol, this model is still widely employed. To illustrate this point, the Haldane model is not the only one currently available [24]. In addition to the model, there have been numerous models that have been shown to be superior such as Luong [25,26] and Edward [27]. As a result of this, the Haldane may be rendered obsolete in some circumstances as a result of the utilization of the more extensive models that are currently available. It is not recommended to make haphazard use of the Haldane model without first doing exhaustive statistical analysis and attempting to fit other models to previously collected data on rate of growth or degradation. In this study, we continue the work by further modeling the influence of substrate or phenol on the growth rate of the bacterium by using different substrate inhibition kinetic models.

## MATERIALS AND METHODS

Data from Fig 1. from the growth of an acclimatized mixed bacterial consortia from an anaerobic batch reactor on phenol [28] was processed using the software Webplotdigitizer 2.5 [29]. It converts the scanned image into digital form and is used by a great number of scholars and is recognized for the accuracy it provides [30,31]. The specific maximum growth rate on phenol at various concentrations of phenol was obtained using a no lag modified logistics model as other primary growth models such as no lag modified Gompertz model failed to fit the growth data (published elsewhere). The ten models of inhibition kinetics are shown in **Table 1**.

**Table 1.** Various mathematical models developed for degradation kinetics involving substrate inhibition of phenol on an acclimatized mixed bacterial consortium from an anaerobic batch reactor.

Author	Degradation Rate	Author
Monod	$\frac{\mu_{max}S}{S + K_s}$	[32]
Haldane	$\frac{\mu_{max}S}{S + K_s + \left(\frac{S^2}{K_i}\right)}$	[33]
Teissier	$\mu_{max} \left( 1 - \exp\left(-\frac{S}{K_i}\right) - \exp\left(\frac{S}{K_s}\right) \right)$	[34]
Aiba	$\mu_{max} \frac{S}{K_s + S} \exp\left(-\frac{S}{K_i}\right)$	[35]
Yano and Koga	$\frac{\mu_{max}S}{S + K_s + \left(\frac{S^2}{K_i}\right) \left(1 + \frac{S}{K}\right)}$	[36]
Han and Levenspiel	$\mu_{max} \left( 1 - \left(\frac{S}{S_m}\right) \right)^n \left( \frac{S}{S + K_s \left( 1 - \left(\frac{S}{S_m}\right)^m \right)} \right)$	[37]
Luong	$\mu_{max} \frac{S}{S + K_s} \left( 1 - \left(\frac{S}{S_m}\right) \right)^n$	[38]
Moser	$\frac{\mu_{max}S^n}{K_s + S^n}$	[39]
Webb	$\frac{\mu_{max}S \left( 1 + \frac{S}{K} \right)}{S + K_s + \frac{S^2}{K_i}}$	[40]
Hinshelwood	$\mu_{max} \frac{S}{K_s + S} (1 - K_p P)$	[41]

Note:  
 $\mu_{max}$  maximal specific growth rate  
 $K_s$  half saturation constant  
 $K_i$  inhibition constant  
 $S_m$  maximal concentration of substrate tolerated  
 $K_p$  product inhibition constant  
 $m, n, K$  curve parameters  
 $S$  substrate concentration  
 $p$  product concentration

### Fitting of the data

Fitting of the inhibition curves using various growth models was carried out using the CurveExpert Professional software (Version 1.6) by nonlinear regression utilizing the Marquardt algorithm.

### Statistical analysis

The following statistical functions were utilized to determine the best models;

The RMSE allows number of parameters' penalty and was calculated using Equation 1, where  $n$  illustrates the number of experimental data, where else  $p$  is the number of parameters calculated by the model and experimental data and values predicted by the model are  $Ob_i$  and  $Pd_i$ , respectively [42]. With the regression line approaching the data points, the root mean square error (RMSE) reduces due to the reduced error in the model. More accurate predictions are generated by a model that has a lower error rate. Comparable in magnitude to the dependent (outcome) variable, the RMSE values span an infinite number of positive infinities. The root mean square error (RMSE) can be employed to assess the extent of imprecision in a statistical model, including regression models. If a value is zero, it signifies that the predicted and actual values are an exact match. The model exhibits superior data fit and generates more precise predictions, as indicated by low RMSE values. In contrast, increased levels indicate a greater magnitude of errors and a reduced number of precise predictions.

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (Pd_i - Ob_i)^2}{n-p}} \quad (\text{Eqn. 1})$$

The  $R^2$  value, also known as the coefficient of determination, was used in linear regression to select the model that provided the best fit. On the other hand, in the case of nonlinear regression, the  $R^2$  does not provide a comparative analysis in situations in which the number of parameters in the various models varies. In order to get around this obstacle, the quality of the nonlinear models was determined by adjusting the  $R^2$  value.  $S_y^2$  is the total variance of the y-variable, while RMS stands for residual mean square. These two terms are used in the adjusted  $R^2$  formula (Equations 2 and 3).

$$Adjusted (R^2) = 1 - \frac{RMS}{S_y^2} \quad (\text{Eqn. 2})$$

$$Adjusted (R^2) = 1 - \frac{(1-R^2)(n-1)}{(n-p-1)} \quad (\text{Eqn. 3})$$

One can measure the relative quality of various statistical models for a given set of experimental data by using the Akaike Information Criterion (AIC). This criterion was developed by Akaike. Instead, data sets that have a large number of parameters or few values should utilize the AIC that has been corrected, which is denoted by the letter AICc [43]. The AICc was determined using the equation that is presented below (Equation 4).

$$AICc = 2p + n \ln \left( \frac{RSS}{n} \right) + 2(p+1) + \frac{2(p+1)(p+2)}{n-p-2} \quad (\text{Eqn. 4})$$

Another statistical measure that is founded on information theory is known as the Bayesian Information Criterion (BIC) (Equation 5), which can be compared to the AICc. Models with the lowest Bayesian information criterion (BIC) are typically preferred over those with higher BICs when choosing from a finite number of models. It has close ties to the Akaike information criteria and is partially based on the likelihood function (AIC). This error function imposes a harsher penalty on the number of parameters than the AIC does [44].

$$BIC = n \ln \frac{RSS}{n} + p \ln (n) \quad (\text{Eqn. 5})$$

The Hannan–Quinn information criterion, often known as the HQC, is an additional error function approach that is based on the information theory (Equation 7). To evaluate how well a statistical model fits data, experts use the Hannan–Quinn information criterion (HQC). It is a common metric to employ when choosing one model over another. In contrast to the LLF, it is connected to Akaike's information criterion. The HQC, like the AIC, includes a penalty function for the total number of model parameters, however it is significantly bigger than the value assigned by the AIC because the equation contains the  $\ln \ln n$  term [45];

$$HQC = n \times \ln \frac{RSS}{n} + 2 \times p \times \ln(\ln n) \quad (\text{Eqn. 7})$$

Both BF and AF were utilized in an effort to evaluate the appropriateness of the models. In order to get a correlation of 1 between the anticipated value and the observed value, the Bias Factor needs to be equal to 1. The Bias Factor and Accuracy Factor originates from predictive microbiology under the food microbiology field and have found applications in modelling

microbial growth that leads to food spoilage [46–53]. A fail-safe model is indicated when the value of the Bias Factor (Equation 8) is greater than 1, and a fail-negative model is indicated when the value of the Bias Factor is less than 1. When compared to 1, a value of Accuracy that is less than 1 indicates a less accurate prediction (Equation 9).

$$\text{Bias factor} = 10 \left( \sum_{i=1}^n \log \frac{(Pd_i/Ob_i)}{n} \right) \quad (\text{Eqn. 8})$$

$$\text{Accuracy factor} = 10 \left( \sum_{i=1}^n \log \frac{|(Pd_i/Ob_i)|}{n} \right) \quad (\text{Eqn. 9})$$

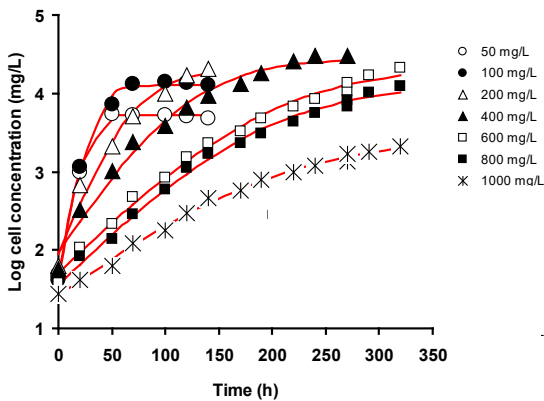
Another parameter-penalized model is MPSD. The Marquardt's percent standard deviation (MPSD). This error function distribution follows the geometric mean error which allows for the penalty to the number of parameters of a model (Equation 10).

$$\text{MPSD} = 100 \sqrt{\frac{1}{n-p} \sum_{i=1}^n \left( \frac{Ob_i - Pd_i}{Ob_i} \right)^2} \quad (\text{Eqn. 10})$$

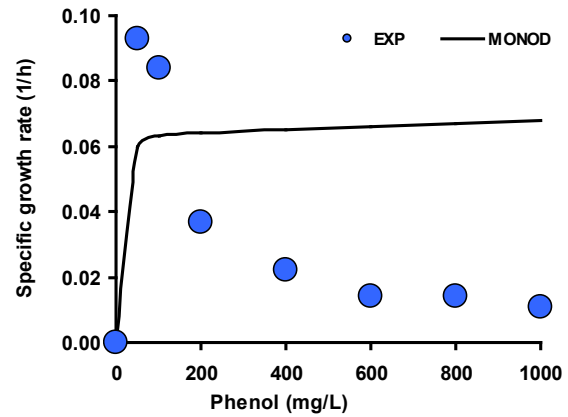
where  $p$  is the number of parameters,  $n$  is the number of experimental data,  $Ob_i$  is the experimental data, and  $Pd_i$  is the value predicted by the model.

## RESULTS AND DISCUSSION

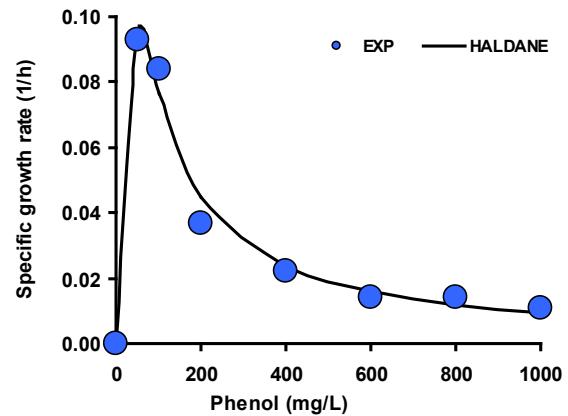
In this study, the specific maximum growth rate on phenol ( $\mu_m$ ) was first obtained using the no lag modified logistics model (Fig. 1). The results of the RMSE, AICc, adjusted  $R^2$ , F-test, and bias and accuracy factor comparisons demonstrate that the Haldane model is the most accurate and precise of the kinetic models considered (Table 2). The resultant fittings (Figs 2 to 11) demonstrate satisfactory fit except for the Monod and Moser models.



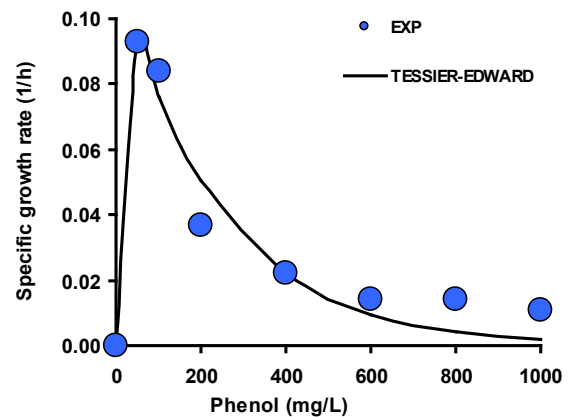
**Fig 1.** The growth curves of an acclimatized mixed bacterial consortia from an anaerobic batch reactor on various concentrations of phenol as modelled using the no lag modified Logistics model.



**Fig 2.** The particular growth data were fitted with respect to phenol concentration using the model of Monod.



**Fig 3.** The particular growth data were fitted with respect to phenol concentration using the model of Haldane.



**Fig 4.** The particular growth data were fitted with respect to phenol concentration using the model of Teissier.

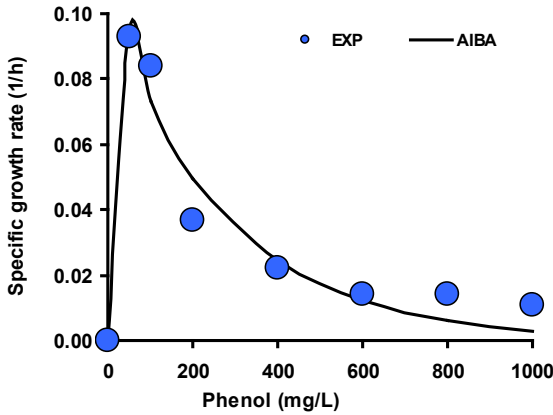


Fig 5. The particular growth data were fitted with respect to phenol concentration using the model of Aiba.

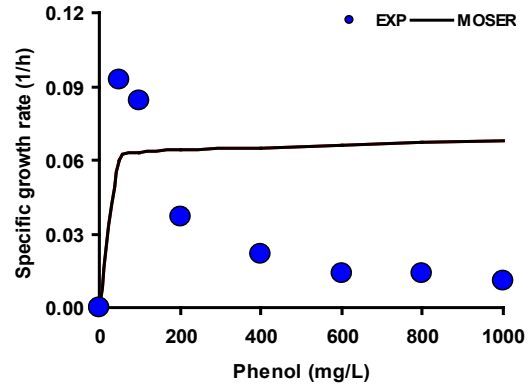


Fig 8. The particular growth data were fitted with respect to phenol concentration using the model of Moser.

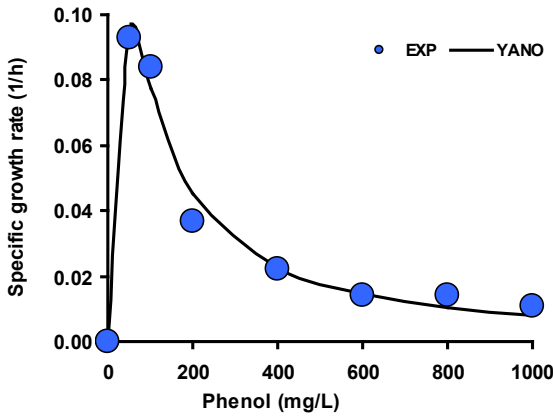


Fig 6. The particular growth data were fitted with respect to phenol concentration using the model of Yano and Koga.

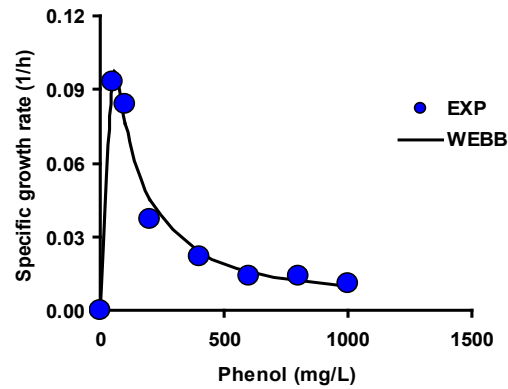


Fig 9. The particular growth data were fitted with respect to phenol concentration using the model of Webb.

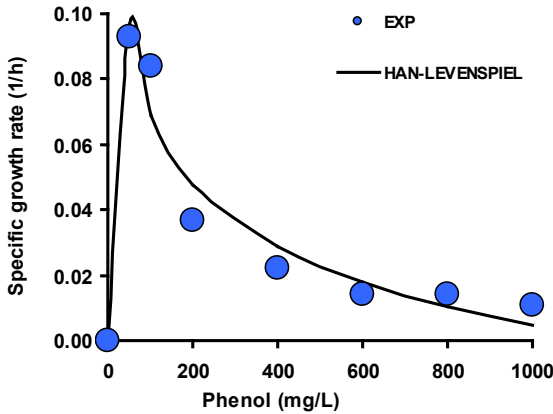


Fig 7. The particular growth data were fitted with respect to phenol concentration using the model of Han and Levenspiel.

Table 1. Statistical analysis of the various fitting models.

Model	p	RMSE	adjR2	MPSD	AICc	BIC	HQC	BF	AF
Luong	4	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.
Yano	4	0.006	0.963	26.39	-39.96	-79.65	-82.11	0.95	1.13
Tessier-									
Edward	3	0.009	0.918	245.12	-51.15	-72.24	-74.09	0.68	1.60
Aiba	3	0.009	0.919	130.50	-51.55	-72.64	-74.49	0.78	1.42
Haldane	3	0.005	0.971	15.04	-60.31	-81.41	-83.25	1.00	1.11
Monod	2	0.046	-3.859	70.46	-35.46	-47.30	-48.53	2.08	2.49
Han and									
Levenspiel	5	0.012	0.800	79.74	27.98	-67.62	-70.70	0.94	1.30
Moser	3	0.077	-5.696	77.18	-17.53	-38.62	-40.47	2.08	2.49
Hinshlewood	4	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.
Webb	4	0.007	0.946	16.68	-37.12	-76.80	-79.26	1.00	1.11

Note:

p no of parameters  
 RMSE Root Mean Square Error  
 AdjR<sup>2</sup> Adjusted Coefficient of determination  
 BF Bias factor  
 AF Accuracy factor  
 n.a. not available

The designated values of the Haldane constants were maximal reduction rate, half saturation constant for maximal reduction and half inhibition constant which are symbolized by  $\mu_{max}$ ,  $K_s$  and  $K_i$  were  $0.157 \text{ hr}^{-1}$  (95% confidence interval 0.072 to 0.231),  $32.042 \text{ mg/L}$  (95% C.I. 14.603 to 49.480) and  $234.095 \text{ mg/L}$  (95% C.I. 181.83 to 286.17), respectively. The output of curve fitting interpolation should not be considered the true value, and the user should be duly informed of this as the true  $\mu_{max}$  should be the point at which the slope's gradient becomes zero; in this instance, the value was  $0.095 \text{ h}^{-1}$  at  $50.1 \text{ mg/L}$  phenol. The equation for the



Haldane model using the values obtained from the fitting is as follows;

$$\frac{0.157S}{S + 32.042 + \left(\frac{S^2}{234.095}\right)}$$

Models like Luong's, Teissier's, and Hans Levenspiel's have been developed to account for the occurrences in which the growth rate approaches zero at very high substrate concentrations where the earlier Monod model could not be used [54]. Overly high concentrations of substrates can have toxic and repressive effects on microbes, stunting their growth. Much of the current use of the Haldane model for modelling the effect of toxic xenobiotics to xenobiotic-degrading bacteria centres predominantly to phenol-degrading microorganisms [55–62]. This is followed by Teissier [63,64,64–66]. It appears that other models were found to be less reported and the reason for this is that in numerous cases only the Haldane model was utilized to model the effect of phenol on the growth or degradation rate of microorganisms on phenol.

In 1930, Haldane presented his model, now known as the Haldane model. The model is thought of as a development of the Monod model. The model includes a third constant,  $K_i$ , to account for substrate concentration-dependent inhibition of the specific growth rate. The substrate concentration at which the specific growth rate is half the maximum growth rate absent inhibition is equal to the inhibition constant or  $K_s$ . Hazardous substrate may slow an organism's specific growth rate at high substrate concentrations. The model can deal with both hazardous and non-hazardous substrates. The Haldane model's strength lies in its ability to characterize all stages of the kinetics of growth rate. The Haldane model was widely utilized because it well described growth rate at both low and high substrate concentration. Before the Haldane model becomes in popular use, the classical Monod model is the most often utilized model.

Jacques Monod first proposed the Monod model in 1942 [67] to explain the correlation between specific growth rate and substrate consumption rate in a bioreactor. Although they are quite similar in appearance, the Michaelis-Menten equation and the Monod equation are based on theory rather than observation. Similar to the Michaelis-Menten expression for enzyme kinetics, the Monod equation for the specific growth rate can be expressed in terms of constants. Methods given for calculating  $v_{max}$  and  $K_m$  for an enzyme reaction can, in theory, also be used to calculate  $\mu_{max}$  and  $K_s$ . Substrate concentration alone or together with biomass concentration can be used to define the model in its various versions. Specifically,  $X$  is biomass concentration,  $K_s$  half saturation constant, specific bacterial growth rate, and  $\mu_{max}$  is the maximum bacterial growth rate. There is no change in either the maximum growth rate or the half saturation constant of bacteria. In the bioreactor, the Monod model presumes that there is only a single substrate restricting growth (Monod, 1942). Kong lists several restrictions [68] on the usefulness of the Monod model [69]. At high substrate concentrations, the first restriction becomes apparent. Maximum specific growth rate is not affected by substrate concentration at high concentration. The second restriction appears when the concentration of the substrate is low. Growth at low substrate concentrations is substrate dependent. Third, the Monod model is inapplicable when the substrate is inhibited [70–72]. Similar to the Michaelis-Menten kinetics model, at low substrate concentrations, the growth rate approaches a first-order with respect to substrate concentrations whilst at elevated substrate concentrations, the growth rate

approaches a zero-order with respect to substrate concentrations. For the Haldane and many substrates inhibition at high concentrations of substrate, the downward slope of the growth rate indicates a negative order of reaction. In many xenobiotics or hazardous compounds bioremediation works, toxic substrates that inhibit bacterial growth and consumption of substrates means that the Monod models will not be useful and the other substrate inhibition models are needed [73–77].

## CONCLUSION

In this work, we found that an acclimatized mixed bacterial consortium from an anaerobic batch reactor's growth rate was significantly impeded at exceedingly high concentrations of phenol, and the majority of discriminatory statistical findings acquired indicated that the Haldane model more accurately represented the growth rate data at various concentrations of phenol. This study demonstrated that the popular Haldane model is often used due to its ability to model inhibitory effects of toxicant, especially phenol to the growth rate of microorganisms.

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